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Improved Method for Determining the n -Value of HTS Bulks

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Abstract— The complete penetration magnetic field B_P is the main feature of a superconducting pellet submitted to an axial applied magnetic field. The electric E - J characteristics of HTS bulk is generally described by a power law $E(J) = E_C(J/J_C)^n$. The influence of the n -value and applied magnetic field rise rate V_b on the B_P of a HTS cylindrical pellet has been presented in a previous paper. The numerical results presented come from numerical resolution of a non linear diffusion problem. With the help of these simulations a linear relationship between B_P , $\ln V_b$ and n -value has been deduced. This comparison allows determining the critical current density J_C and the n -value of the power law based on direct measurement of B_P in the gap between two bulk HTS pellets. In this paper, an improvement of this method is presented. The influence of geometric parameters R and L is studied to give generality to the relationship between B_P , V_b and n -value. Previous B_P formula is confirmed by these new simulations. To correctly connect simulation and experimental results, the influence of spacing e between bulks is studied and presented. A relationship between B_P and measured complete penetration magnetic field B_{PM} is determined.

Index Terms—Critical current density, magnetic field diffusion, superconductors.

I. INTRODUCTION

THE use of high temperature superconductor (HTS) bulks for electric motors, generators or magnetic levitation systems is now feasible due to high critical current density and progress of cryogenics [1]–[7]. For low temperature superconductors (LTS) or HTS materials used at low temperatures, the critical state model (CSM) is used [8]. Since in the CSM J can only take well defined values such as 0 or J_C (critical current density) that do not depend on the rate of variation of the externally applied field. Because of this simple relationship, J_C can be determined by magnetization experiments [9], [10].

If a cylindrical HTS pellet is submitted to an uniform axial applied magnetic field $B_a(t)$ as in Fig. 1, the magnetic field at the center of the pellet $B_0(t)$ starts to rise after some time delay T_p , related to the moment at which B_a reaches B_P , Fig. 2. For cylinders, and assuming CSM applies, an analytic expression

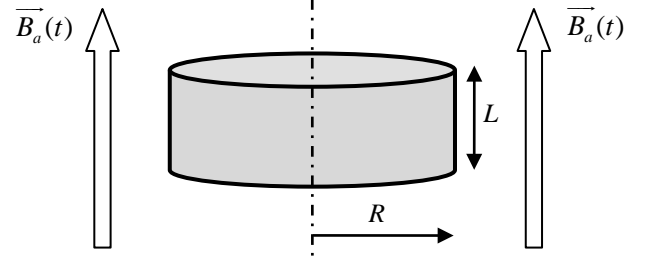


Fig. 1. Bulk superconducting pellet of cylindrical shape submitted to a uniform axial magnetic field.

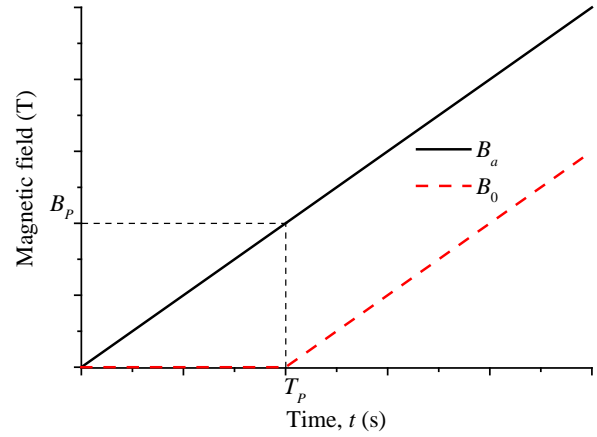


Fig. 2. Linear growth of the applied magnetic field B_a and the theoretical magnetic field B_0 at the center of the pellet versus time t .

for the complete penetration field, named B_{PB} , can be obtained based on the application of the Biot–Savart law [10]–[12]:

$$B_{PB} = \frac{\mu_0 J_C L}{4} \ln \left(\frac{\sqrt{R^2 + \left(\frac{L}{2}\right)^2} + R}{\sqrt{R^2 + \left(\frac{L}{2}\right)^2} - R} \right) \quad (1)$$

where L is the length of cylinder and R is its radius.

In the case of HTS used at “high temperatures”, typically above 50–60 K, a power law model better represents the $E(J)$ characteristic of the materials than the CSM model [11]–[17]. The power law model is typically written as:

$$E = E_C \left(\frac{J}{J_C} \right)^n = \frac{E_C}{J_C} \left(\frac{J}{J_C} \right)^{n-1} J \quad (2)$$

The critical current density J_C and the n -value depend on temperature, magnetic field and there is an inhomogeneity of J_C over the volume [14]. However, in this paper J_C and n -

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value are assumed constant. The determination of the J_C and n parameters defining the power law model for a given bulk superconductor is not simple. Typical n -values vary between 10 and 50 at 77 K [18]–[20]. The calculation of the magnetization of superconducting samples assuming power law model generally requires numerical simulations. A new method of determination of J_C and n , by studying the influence of the n -value and the applied magnetic field rising rate V_b on the complete penetration magnetic field B_P is presented in [11]. For cylinders, and assuming power law model, an analytic expression for the complete penetration field, named B_P , has been deduced:

$$B_P = B_{PB} \left(1 + \frac{\alpha \ln V_b + \beta}{n} \right) \quad (3)$$

During all the simulations, the applied magnetic field $B_a(t)$ was a linearly increasing field, as shown in Fig. 2. The pellet has a radius R of 10 mm and a thickness L of 10 mm, which corresponds to the pellets used in the experimental part of this work. The value of J_C chosen was 100 A/mm², which is a realistic value for HTS bulks at 77 K. For this particular case [11], $\alpha = 1.2$ and $\beta = 3.4$ have been deduced from simulation curves. In this paper, the influence of the geometrical parameters R and L is studied in order to give a more general formula (3).

Based on (3), the power law model parameters J_C and n of a cylindrical sample are determined from experimental measurements as described in [11]. In order to use the results derived above by simulations, one need to measure the complete penetration magnetic field B_P in the pellets. The main idea of our method is to separate the studied pellet in two pellets to allow deducing B_P from measurement of the complete penetration magnetic field B_{PM} between these two pellets. The magnetic field is detected with an axial Hall probe placed on the central axis of two HTS pellets, Fig. 3. The cylindrical HTS pellets used in this experiment were YBCO pellets with 10 mm of radius and 5 mm of thickness. In the simulation, the thickness of the corresponding pellet was taken as L , i.e. the sum of the two half-pellets. To correctly connect simulation and experimental results, the influence of the Hall probe thickness e must be taken into account. In this paper, the influence of the spacing e between the bulk pellets is presented.

II. INFLUENCE OF CRITICAL CURRENT DENSITY AND GEOMETRIC SIZES ON B_P

In (3), B_P is the product of two functions. The first one is B_{PB} and the second one a function of V_b and n -value. In [11], the following assumptions are assumed: J_C and the geometric parameters R and L are only included in B_{PB} and excluded from the second one. To check these assumptions, new simulations were made with different J_C and different L/R ratios. In these simulations one HTS pellet is submitted to a linearly increasing applied magnetic field $B_a(t)$ as shown in Fig. 2. As shown in a previous article [10], thermal effects can be neglected in our study. In these simulations chosen n -

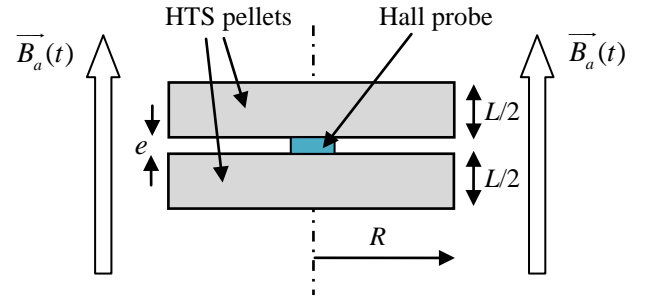


Fig. 3. Hall probe location between the two HTS pellets.

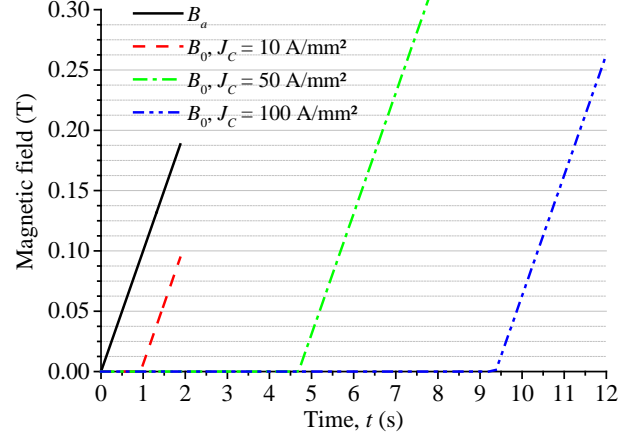


Fig. 4. Applied magnetic field and magnetic field at the center of the pellet with $R = 10$ mm, $L = 10$ mm, $n = 15$, $V_b = 1$ T/s and different J_C .

values are 15, 25 and 50.

A. Simulations with different values of J_C

In these simulations, $R = 10$ mm, $L = 10$ mm, $n = 15$, $V_b = 1$ T/s, and $B_a(t)$ and $B_0(t)$ are represented in Fig. 4 for three different values of J_C , 10 A/mm², 50 A/mm² and 100 A/mm². Fig. 4 clearly shows that T_P is proportional to J_C . The same conclusion is obtained with other n -values. As $B_P = V_b \cdot T_P$, B_P is also proportional to J_C . B_{PB} can also be calculated from B_P using (3) and then be compared to (1). Using (3) with $n = 15$, one can calculate $B_{PB} = 0.91$ T with $J_C = 100$ A/mm², and $B_{PB} = 0.091$ T with $J_C = 10$ A/mm². The same values of B_{PB} were obtained using (1). These results are confirmed for different rise rates from 0.01 T/s to 1000 T/s. These results prove that the assumption that J_C is included in B_{PB} is valid.

B. Simulations with different L/R ratios

In these simulations, the n -values are chosen equals to 15, $R = 10$ mm and the L/R ratios of the pellet vary from 0.5 to 3. These values are commonly observed on commercial HTS pellets. For $n = 15$, $B_a(t)$ and $B_0(t)$ are represented in Fig. 5 for six different values of L/R ratios. From these curves, B_P values are deduced. As expected, B_P increases with the L/R ratio at a given R . For these L/R ratios, B_{PB} is calculated from (1). Finally, the ratio B_P/B_{PB} is calculated and represented on Fig. 6. For all the rise rates and the n -values tested, B_P/B_{PB} remains constant whatever the L/R ratio. It demonstrates that the geometric parameters R and L only affect B_{PB} and not the parameters α and β of (3).

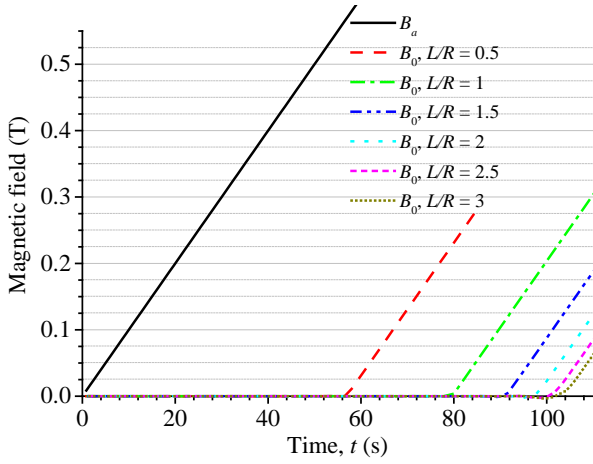


Fig. 5. Applied magnetic field and magnetic field at the center of the pellet with $R = 10$ mm, $n = 15$, $V_b = 0.01$ T/s, $J_C = 100$ A/mm² and different L/R ratios.

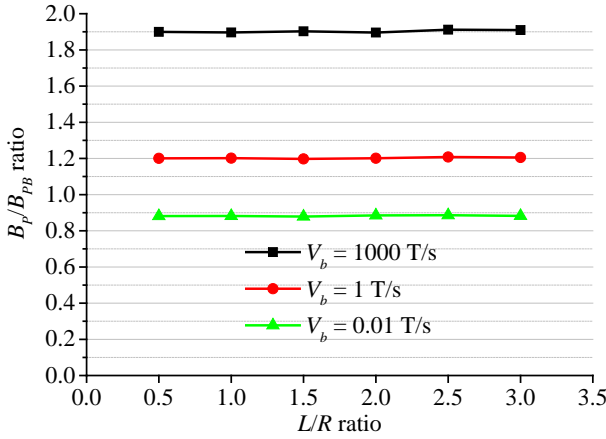


Fig. 6. B_P/B_{PB} ratio vs L/R ratio for $n = 15$, $J_C = 100$ A/mm² and different V_b .

III. INFLUENCE OF THE SENSOR THICKNESS ON N -VALUE AND J_C DETERMINATION

As described in [11], experiments results give the measured complete penetration magnetic field B_{PM} and not B_P . So it is crucial to find relationship between both. In order to obtain it, simulations have been made with two HTS pellets and different spacings corresponding to the typical thicknesses of Hall probes, i.e. $e = 0.5$ mm and 1 mm. In this paper, we called B_{PM} the measured complete penetration magnetic field obtained by simulations of realistic cases. Then, we compared the results with those of a single pellet without Hall probe, i.e. $e = 0$ mm from which we have deduced B_P . In previous study [11], only one value of L and one value of V_b were used in simulations. In this present work, results with different V_b values and different L values are presented. This allows giving generality to this work. The applied magnetic field and the magnetic field at the center between the two pellets, with $n = 15$, $V_b = 1000$ T/s, $J_C = 100$ A/mm², $R = 10$ mm, $L = 10$ mm and different sensor thicknesses are presented in Fig. 7. As a previous study [10] showed, the shape of magnetic field at the center, between the two pellets for $e = 0.5$ and 1 mm, is not linear around T_P even if $B_a(t)$ is linear, Fig. 7. To allow the determination of the values of T_P for $e = 0.5$ and 1 mm, dash lines are superimposed on B_0 in

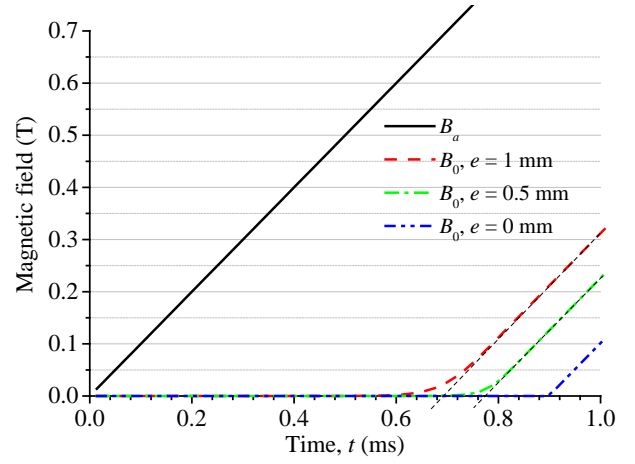


Fig. 7. Applied magnetic field and magnetic field at the center of the pellet with $R = 10$ mm, $n = 15$, $V_b = 1000$ T/s, $J_C = 100$ A/mm², $L = 10$ mm, and two different sensor thicknesses, $e = 0.5$ and 1 mm

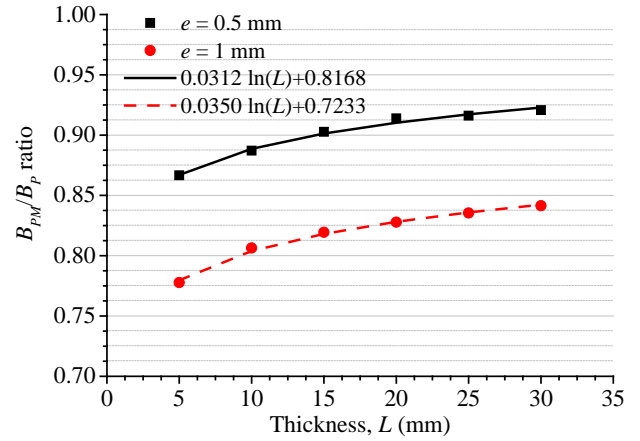


Fig. 8. B_{PM}/B_P ratio for $e = 0.5$ and 1 mm, $R = 10$ mm, $n = 15$, $J_C = 100$ A/mm², $V_b = 1000$ T/s.

Fig. 7. From these values of T_P for $e = 0.5$ and 1 mm, values of B_{PM} are deduced. Finally B_{PM}/B_P is calculated for $e = 0.5$ mm and 1 mm and different values of L , Fig. 8.

Two relationships between B_{PM}/B_P and L are deduced:

$$\frac{B_{PM}}{B_P}(e = 0.5 \text{ mm}) = 0.0312 \ln(L) + 0.8168, \quad (4)$$

$$\frac{B_{PM}}{B_P}(e = 1 \text{ mm}) = 0.0350 \ln(L) + 0.7233. \quad (5)$$

Equations (4) and (5) remain the same for different n -values and different values of rise rate V_b . So (4) and (5) are not dependant of n and V_b . However, (4) and (5) are available only for $R = 10$ mm. Therefore, for each value of R new relationship between B_{PM} and B_P have to be calculated. In this work we want to show that it is possible to calculate B_P from measurement of B_{PM} . Future work has to give more general relationships between B_{PM}/B_P and geometric parameters e , R and L .

IV. CONCLUSION

The validity of our formula for the complete penetration magnetic field is proved and reinforced by many simulations.

The influence of sensor thickness on experimental determination of n -value is presented. Relationship between theoretical B_P and measured B_{PM} is determined. In this method, constant J_C and n -value are assumed. In future work, taking into account $J_C(B)$ with this method may be a new goal.

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